MATH 15 PRACTICE MIDTERM S'01, May 2, 2001

Unless told otherwise, your answers must be carefully justified. Remember that it is not enough to have a correct answer, you must show how you got it. Neat work, clear and to-the-point explanations will receive more credit than messy, chaotic answers. You may not use books, notes, and calculators on this exam, but you may have a 3" by 5" handwritten cheat sheet.

- 1. (a) You ride your bicycle from UCSB to Santa Barbara harbor (12 miles). Part of the way, you ride at 15 mph, then you walk your bike at 3 mph. Find a function f(d) that gives the total travel time in hours as a function of d, the part of the distance walked (in miles).
 - (b) Find f(f(2)) and $f^{-1}(3)$ if

$$f(x) = \frac{x+2}{x-1}.$$

- 2. (a) Find an equation of the line through (2, 0) and (-2, 2).
 - (b) Find the intersection of y = 3x + 1 and x + y = 1. Check your answer.
- 3. (a) Show that

$$1 - 3\log 2 = \log\left(\frac{5}{4}\right)$$

(b) Let $a = \log x$ and $b = \log y$. Express in terms of a and b

$$\log\left(\frac{\sqrt[3]{x^2}}{\sqrt[5]{y}}\right).$$

4. Graph the function

$$f(x) = \begin{cases} x+1 & \text{if } x < 0 \\ x-1 & \text{if } 0 \le x < 2 \\ x+1 & \text{if } 2 \le x \end{cases}.$$

Find f(f(3)) and $f^{-1}(-2)$.

5. Find the domain and the range of

$$f(x) = \frac{2}{\sqrt{1 - \frac{1}{x}}}.$$

- 6. You have some radioactive material whose mass is decaying exponentially. After two weeks, there is 200 g left, after five weeks only 25 g.
 - (a) Find a function f(t) that describes the amount of the material after t weeks.
 - (b) How much material was there initially?
 - (c) What percentage of the material decays in a week?
 - (d) Assuming the decay were linear at a rate of 25%/week, how much of the material would you have after five weeks?