

MCS 220, Introduction to Analysis: Theory of Calculus

Fall 2019, 10:30–11:20 MTuThF, OHS 321

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Office hours: 2:30-3:30 on Mon and Thu, 3:15-4:15 on Tue, and 12:30-1:25 on Fri.

Prerequisites: Completion of calculus II (MCS-122). You may find it really useful to have taken MCS-228, or taking it concurrently, but it is not a requirement.

Required text: William F. Trench. Introduction to Real Analysis, Free Hyperlinked Edition 2.04. This is a free textbook, available as a pdf via a link from the class website.

Course objective: This is an introductory course in single-variable real analysis. We will study functions of a single variable whose domain and codomain are subsets of the real numbers. You certainly learned about those in your calculus courses too, but now we are taking a more sophisticated look. We will revisit some of the topics you have likely seen in calculus, such as functions, limits and convergence, continuity, differentiation and integration, and sequences and series of real numbers and real functions. We will approach these in a more rigorous fashion than in calculus, including doing many proofs about why calculus works the way it does. In fact, one of the major goals of the course—other than learning real analysis—is to sharpen your proof writing skills. You will have to be able to state precise definitions, come up with examples, prove theorems covered in class and in the text, and prove or disprove unfamiliar statements in real analysis whose level and sophistication are comparable to the material in lecture and on the homework.

Website: <https://homepages.gac.edu/~ituba/mcs220f19>. I will also use Moodle to post your grades periodically.

Class attendance: This is not distance education. You are expected to attend and participate in every class. If you skip class you will miss the chance to learn skills that will be tested on the exams. If you keep skipping class, I will think that you are not serious about your education and will remember that when I assign your grade at the end of the semester.

On work outside class: Have you ever wondered why taking three classes (12 units) qualifies you as a full time student? That's only 10 hours per week in class. The reason is that you are expected to do a lot of work on your own outside class. In fact, the rule of thumb of college education is that for every hour you spend in class, you should expect to spend three hours studying outside class. That is how 12 units makes full time: 10 hours in class and 30 hours studying outside class each week. That means you'll need to spend about 10 hours a week studying outside the classroom for this course. That is if you are well-prepared for the course. If your math background is lacking, then you'll have to spend more time. I am not kidding.

Homework and reading will be posted on the class website regularly. You will be able to follow the progress of the course using the website. HW is an essential part of your learning. Take it very seriously. It is extremely important that you keep up with the HW. If you do not, you will quickly find yourself lost in class and at a great disadvantage during exams. Treat the HW as a learning opportunity, rather than something you need to get out of the way. Reread, revise, and polish your solutions until they are correct, concise, efficient, and elegant. This will really deepen your understanding of the material. You won't do well in a math class without doing all of the HW. Attending class and reading your textbook are necessary but not sufficient conditions for passing the course.

Mostly of your homework will consist of exercises in the textbook. Your work on these exercises will be tested on quizzes and exams. Every quiz and half of every exam will consist of exercises straight from this kind of homework. After the due date, they can show up on quizzes/exams. I strongly suggest that you write up and turn in your homework by the due date. I will correct your work but will not assign a score to it. This is so you treat the homework as a learning opportunity rather than a means of evaluation. In fact, you can turn in your homework to me any time for feedback. I will comment on it and turn it back to you as soon as I can. If you'd like, you can then correct your mistakes and turn it in again for me to check.

There is an obvious winning strategy. Do the HW, seek feedback on it, revise it, and keep your HW notes neat and organized. The familiarity you gain with the exercises by doing this will let you do the quizzes with ease. It will also let you complete half of each exam quickly and move onto the other half of the exam. The experience you gain by keeping up with your homework will be invaluable in doing that other half of the exam. On the other hand, if you do not keep up with your HW, you will face many unfamiliar problems under time pressure on quizzes and exams. This is very difficult and your grade will likely reflect it. Clearly, if you don't turn in homework, I can't give you feedback on your work, no matter how much I want.

Collaboration on the HW: Limited collaboration with your fellow students in the class is OK. But see the section on Academic Integrity! The idea is to let you discuss and critique each other's ideas and not to let you split the workload. Keep collaboration constructive and reasonable. You should fully understand the solution and write it up on your own. Your understanding of the material will be tested on the exams.

If you are approached by another student from the class who wants to copy your HW notes, think twice before generously sharing. You will feel bad if your crafty buddy outscores you on an exam by exploiting your and everybody else's collective wisdom without doing work of his/her own.

Discussion sections: I strongly encourage you to organize a weekly session to work with (not copy from!) your fellow students on problems in class and on the homework. This will help you keep up with your work and get ideas and feedback from others who are grappling with the same exercises as you. You may find that the sense of companionship motivates you to work.

Quizzes: We will have a quiz on average every one and a half to two weeks. It will be straight from the homework. It is your responsibility to come to class, so if you miss a quiz because you are not there, you will usually not be allowed to make it up. But your lowest quiz score will be dropped. If you miss more than one quiz, the missed quiz will count as a score of 0. If you miss more than one quiz and you have a compelling and documented excuse, let me know, and be prepared to show documentation for your excuse. Skipping class is not a compelling excuse.

Exams: There will be two in-class exams on Oct 11 and Nov 8, as well as a final exam. If you skip an exam, you will normally not be able to make it up, unless you have a compelling (e.g. medical) and documented excuse. Forgetting that there is an exam or being unprepared for it are not considered compelling excuses. Your in-class exam score will be computed as $\frac{2}{3}(\text{higher score}) + \frac{1}{3}(\text{lower score})$.

Final exam: 10:30-12:30 on Wed, Dec 18 in OHS 321. The final exam is an important part of your obligations at Gustavus. Do not make travel/vacation plans that prevent you from taking the final exam at the time assigned by the registrar. If you have more than two final exams scheduled for the same day, let me know well in advance.

Grading scheme:

Quizzes	25%
In-class exams	45%
Final exam	30%

A score of 80% or more will guarantee an A- or better, 60% a B- or better, 40% a C- or better, and 20% a D- or better.

On independent work: Problem solving skills are developed by practicing a lot, not by watching other people solve problems. Learning math is much like learning to ride a bicycle in that you learn by doing it and not by watching someone else do it. Expecting to learn math without doing exercises on your own is like expecting to learn to ride a bicycle without ever sitting on a bicycle. Attending class and reading the textbook won't be enough to do well on the exams. You should work through every example and argument in the book and in your class notes and expect to have to re-read everything several times. It's slow, but then your reading list for this class is short.

On academic integrity: Using unauthorized aids—including help from another person—on exams and to complete assignments constitutes cheating. Representing someone else's work as your own—even if you make minor changes to it, or reword it—is plagiarism. Cheating and plagiarism are violations of academic integrity and university policy. The consequences are serious, ranging from receiving a failing grade on an assignment in question to expulsion from the College. Don't do it, it's not worth it. If you are in doubt whether what you are doing is legitimate, it is better to ask me.

According to the College's Academic Honesty Policy and the Honor Code (https://gustavus.edu/general_catalog/current/acainfo), it is your responsibility not only to not commit any act of academic dishonesty yourself, but also to report every instance of academic dishonesty that you know of.

Quality of work: It is important that you work neatly on the assignments. The quality of your work will affect your grades on the exams. Quality has to do with how easy it is for someone else to read your solution to a problem. It is not enough to do the math right, you must also communicate it well.

Students with disabilities: Gustavus Adolphus College is committed to ensuring the full participation of all students in its programs. If you have a documented disability, or you think you may have a disability of any nature (e.g., mental health, attentional, learning, chronic health, sensory, or physical) and, as a result, need reasonable academic accommodation to participate in class, take tests or benefit from the College's services, then you should speak with the Accessibility Resources staff, for a confidential discussion of your needs and appropriate plans. Course requirements cannot be waived, but reasonable accommodations may be provided based on disability documentation and course outcomes. Accommodations cannot be made retroactively; therefore, to maximize your academic success at Gustavus, please contact Accessibility Resources as early as possible. Accessibility Resources (<https://gustavus.edu/advising/disability>) is located in the Center for Academic Resources and Enhancement. Accessibility Resources Coordinator, Katy Clay, (clayk@gustavus.edu or x7197), can provide further information.

If you need special arrangements, let me know well in advance so we can plan to accommodate your needs.